

The density of seawater as a function of salinity (5 to 70 g kg⁻¹) and temperature (273.15 to 363.15 K)

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Abstract. New seawater density measurements were made as a function of temperature $T=(273.15$ to $363.15)$ K and salinity (5 to 70 g kg⁻¹). The measurements ($N=230$) from $T=273.15$ to 313.15 K and Practical Salinity (S) from 0 to 40 were found to be in good agreement ($\sigma=0.0036$ kg m⁻³) with the equation of state of seawater (Millero and Poisson, 1981) made on samples with a known chlorinity (Cl). These results indicate that the Practical Salinities (S) are in agreement to within ± 0.003 kg m⁻³ with the values calculated from the Chlorinity, $S_{Cl}=1.80655$ Cl. The measurements from 298.15 to 363.15 were used to extend the equation of state to high temperatures and salinities. All the densities were made relative to pure water ($\rho-\rho^0$ where ρ^0 is the density for pure water) were fitted to equations of the form

$$(\rho - \rho^0)/(\text{kg m}^{-3}) = AS_A + BS_A^{1.5} + CS_A^2$$

where A , B , and C are functions of temperature and S_A (g kg⁻¹) is the absolute salinity, $S_A=(35.16504/35)S$ g kg⁻¹. The fitted results from $S_A=0$ to 50 g kg⁻¹ and $T=273.15$ to 313.15 K ($N=242$) gave standard errors of 0.0037 kg m⁻³. The fitted results from 298.15 to 363.15 K ($N=280$) gave standard errors of 0.0063 kg m⁻³ and all the results ($N=522$) from 273.15 to 363.15 K gave standard errors of 0.0063 kg m⁻³. The earlier density measurements (Millero et al., 1976b; Poisson et al., 1980) used to determine the equation of state of seawater (Millero and Poisson, 1981) were combined to derive equations that are valid from 273.15 to 313.15 K and 273.15 to 363.15 K. The standard errors of these fits are respectively, 0.0038 kg m⁻³ ($N=713$) and 0.0063 kg m⁻³ ($N=962$). These new measurements expand

the equation of state of seawater to a wider range of temperature (273.15 to 363.15) K and absolute salinity (0 to 70 kg m⁻³).

1 Introduction

The original one atmosphere density measurements used to determine the equation of state of seawater (Millero and Poisson, 1981) were made on seawater of a known Chlorinity (Cl). The salinities of these samples were determined using the relationship

$$S_{Cl} = 1.80655Cl \quad (1)$$

This relationship may or may not be valid at the present time (Millero et al., 1976a). For example, the differences in the Practical Salinity (S) and Chlorinity salinity (S_{Cl}) calculated from Eq. (1) may vary by as much as 0.0055 (Fig. 1). This difference is equivalent to an error in density of ± 0.0041 kg m⁻³.

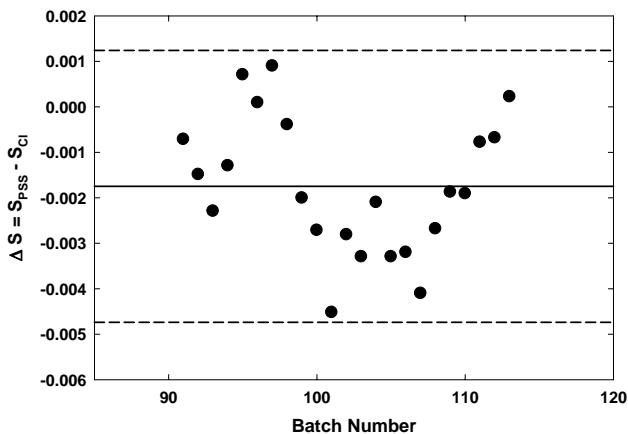
The present one atmosphere equation of state for seawater is limited to Practical Salinities from 0 to 40 and temperatures from 273.15 to 313.15 K. The equation was derived from the measurements of Millero et al. (1976b) and Poisson et al. (1980). A summary of these measurements are given in Table 1. The equation of state derived from the studies of Millero et al. (1976b) and Poisson et al. (1980) had a $1\sigma=0.0035$ kg m⁻³ similar to the individual studies. Poisson and Gadhoumi (1993) have extended the range to higher Practical Salinities ($S=50$) from 288.15 to 303.15 K. They give equations that represent this data with standard errors close to those of the equation of state (Millero and Poisson, 1981). Measurements to a higher temperature are not available at the present time. As the physical chemical properties



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Table 1. Summary of the 1 atm density measurements made on seawater.

| Author | Number | Std Error (1 σ) | Temperature | Salinity |
|-----------------------------|--------|------------------------------|--------------------|----------|
| Millero et al. (1976b) | 122 | 0.0035 kg m ⁻³ | 273.15 to 313.15 K | 1 to 40 |
| Poisson et al. (1980) | 344 | 0.0035 kg m ⁻³ | 273.45 to 303.15 K | 5 to 41 |
| Poisson and Gadhoumi (1993) | 79 | 0.0064 kg m ⁻³ | 288.15 to 303.15 K | 35 to 50 |
| This Study | 242 | 0.0037 kg m ⁻³ | 273.15 to 313.15 K | 5 to 50 |
| All Combined | 713 | (0.0036 kg m ⁻³) | | |
| This Study | 280 | 0.0063 kg m ⁻³ | 273.15 to 363.15 K | 4 to 70 |
| All Combined | 962 | (0.0063 kg m ⁻³) | | |

**Fig. 1.** The differences between the Practical Salinity (S_{PSS}) and the value calculated from the Chlorinity ($S_{Cl}=1.80655 Cl$) for the last series of Standard Seawater where Chlorinity was measured (P91 to P113). The dotted lines are 2σ .

of seawater are known to higher temperatures (Millero and Pierrot, 2005; Feistel, 2008), there is a need for density measurements at higher temperatures and salinities.

In this paper, measurements of the density of seawater on the Practical Salinity Scale (S) have been made from 273.15 to 315.15 K and are compared to those calculated from the equation of state (Millero and Poisson, 1981). New measurements of the density of seawater to 363.15 K as a function of absolute salinity, S_A from 0 to 70 g kg⁻¹ are also reported. This study is part of a work to extend the equation of state of seawater over a wider range of temperature and salinity (Feistel, 2008). The results will be useful in examining the use of ionic interaction models (Pierrot and Millero, 2000) to estimate the density over a wide range of temperature and ionic strength and in the future to examine the PVT properties of hydrothermal waters.

2 Experimental methods

The seawaters used in this study were Standard Seawater ($S=35.00$) and surface Gulf Stream seawater ($S=36.10$). Both waters have low nutrient concentrations and had densities that agreed at similar salinities to ± 0.003 kg m⁻³. Solutions at low salinities were obtained by adding ion exchange water by weight and the high salinities by slowly evaporating the samples. No visible precipitation appeared during the sample preparation. The Practical Salinities were measured with an Autosol salinometer calibrated with Standard Seawater. The precision of the Practical Salinity is 0.0005 on a given sample. The absolute salinities of the evaporated samples were back calculated from the weight of the added water needed to dilute it to a salinity range that can be measured by conductivity and density at 298.15 K. The salinities of the evaporated samples are estimated to be accurate to ± 0.003 g kg⁻¹.

The densities were measured on a Paar 500 vibrating tube densimeter at a fixed temperature (± 0.003 K) determined with a Platinum thermometer in the instrument. The densimeter is calibrated with deionized water (Millipore SuperQ) and dry air. The measurements made at high temperatures were made on degassed samples heated to 363.15 K to avoid bubble formation in the instrument. The measurements were then made from 263.15 to 298.15 K. Densities made on Standard Seawater were repeatable to $1\sigma=0.003$ kg m⁻³ from 273.15 to 323.15 K and agree with values calculated from the equation of state (Millero and Poisson, 1981) to ± 0.0035 kg m⁻³ from 293.15 to 313.15 K. The measurements at temperature above 323.15 K have an estimated uncertainty of ± 0.006 kg m⁻³ based on repeat measurements of the same sample. All of the measurements were made relative to the density of water which is based on the equations of Kell (1975) adjusted to the 1990 temperature scale (Spieweck and Bettin, 1992). These are the densities that are embedded in the densimeter. The values of the relative densities ($\rho-\rho^0$) are not affected by densities used in the calibration of the system. The measured water values from 273.15 to 363.15 K agreed to the calculated values to

$\pm 0.002 \text{ kg m}^{-3}$. Since the density of water (ρ^0) in the original equation of state of seawater is based on the less reliable water equations of Bigg (1967) and the values used in the instrument, all of our measurements are reported and compared to the equation of state of seawater (Millero and Poisson, 1981) in terms of the differences in the density of seawater and water ($\rho - \rho^0$) kg m^{-3} .

A number of density measurements on deep waters in the Atlantic (Millero et al., 1976a; 1978), Indian (Poisson et al., 1981; Millero et al., 2008a), and Pacific oceans (Millero et al., 1978; 2009) and the Red (Poisson et al., 1981) and Baltic Seas (Millero and Kremling, 1976) are higher than the values determined from the equation of state (Millero and Poisson, 1981). This is attributed to the added salts to seawater from the dissolution of $\text{SiO}_2 (s)$ and $\text{CaCO}_3 (s)$ and the addition of CO_2 and nutrients from the mineralization of organic matter (Brewer and Bradshaw, 1975; Millero, 2000). Since the conductivity salinity does not respond to all the components in seawater, it is useful to examine the physical properties in terms of the absolute salinity (Millero et al., 2008b; Feistel, 2008). The absolute salinity (g kg^{-1}) is defined (Millero et al., 2008b) by

$$S_A = S_R + \Delta S \quad (2)$$

where the Reference Salinity (S_R) is related to the Practical Salinity (S) by

$$S_R = (35.16504/35) \text{ g kg}^{-1} \times S \quad (3)$$

and ΔS is the increase due to added salts (Brewer and Bradshaw, 1975; Millero, 2000; Millero et al., 2008b). The values of ΔS can be estimated by determining the added Si, Ca, NO_3 , PO_4 and TCO_2 to seawater (Millero et al., 2008a; 2009). It can also be estimated (Millero et al., 2009) from the differences between the measured densities and the values determined from the equations of state using the approximate equation

$$\Delta S_A / (\text{g kg}^{-1}) = \Delta \rho / (\text{kg m}^{-3}) / (0.752 \text{ g kg}^{-1}) \quad (4)$$

where $\Delta \rho = \rho$ (measured) $- \rho$ (calculated from the equation of state) at 25°C . For seawater with no added salts the values of S_A are equal to the Reference Salinity S_R and can be estimated from the Practical Salinity using Eq. (3).

3 Results and discussion

The densities made in this study are given in the Appendix Tables A1 and B1. Two sets of measurements were made from 273.15 to 313.15 K and $S_A = 4$ to 50 g kg^{-1} and from 298.15 to 363.15 K and $S_A = 4$ to 70 g kg^{-1} . The first series of density measurements were made on Standard Seawater ($S = 35.00$, Batch 90–115) and Gulf Stream seawater evaporated and diluted from $S_A = 4$ to 42 g kg^{-1} and from 273.15 to 313.15 K. The measured densities ($N = 230$) are compared

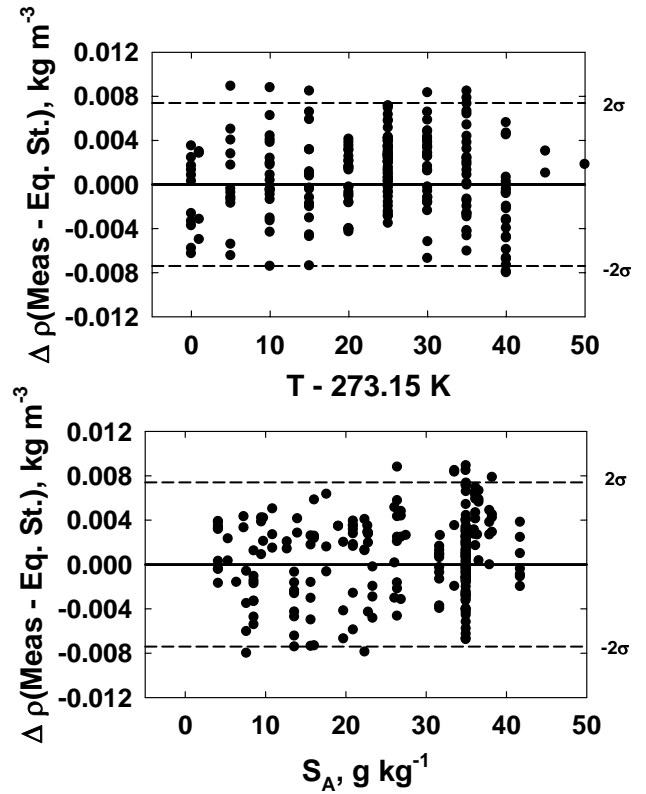


Fig. 2. The differences in the measured ($N = 230$) densities ($\rho - \rho^0$, kg m^{-3}) with those calculated from the equation of state (Millero and Poisson, 1981) as a function of temperature and salinity ($\sigma = 0.0036 \text{ kg m}^{-3}$).

to the values calculated from the equation of state (Millero and Poisson, 1981) as a function of temperature and salinity in Fig. 2. The standard error between the measured and calculated values was 0.0036 kg m^{-3} . This is similar to the errors in the repeat density measurements ($\pm 0.003 \text{ kg m}^{-3}$) on the same sample and indicates that the salinities calculated by conductivity (S) and Chlorinity (S_{Cl}) are in agreement to $\pm 0.004 \text{ g kg}^{-1}$. It should be pointed out that our measurements made at salinities above 40 are higher by as much as 0.064 kg m^{-3} with the measurements of Poisson and Gadhoumi (1993) at 288.15, 298.15 and 303.15 K.

The internal consistency of the measurements was examined by fitting the relative densities to an equation of the form

$$(\rho - \rho^0) / (\text{kg m}^{-3}) = AS_A / (\text{g kg}^{-1}) + B \{S_A / (\text{g kg}^{-1})\}^{1.5} + C \{S_A / (\text{g kg}^{-1})\}^2 \quad (5)$$

The variable A , B and C are functions of temperature (T/K)

$$A = a_0 + a_1(T/\text{K} - 273.15) + a_2(T/\text{K} - 273.15)^2 + a_3(T/\text{K} - 273.15)^3 + a_4(T/\text{K} - 273.15)^4 + a_5(T/\text{K} - 273.15)^5 \quad (5a)$$

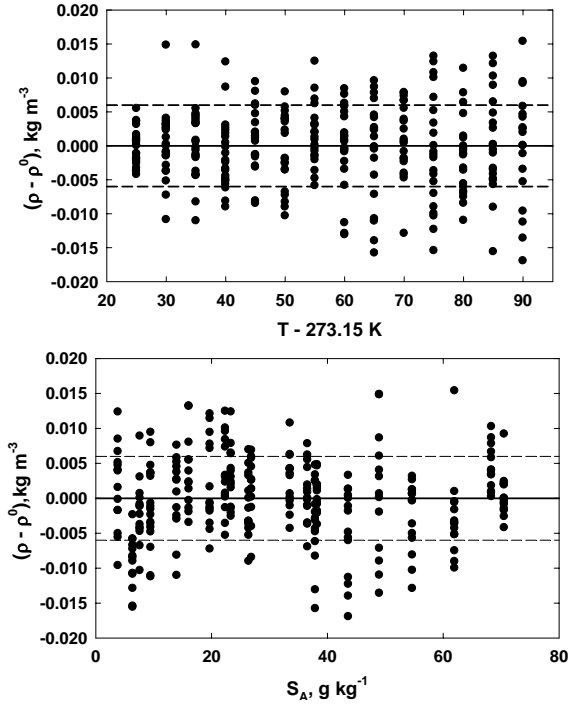


Fig. 3. The differences between the measured ($N=522$) and calculated densities ($\rho-\rho^0$, kg m^{-3}) from 273.15 to 363.15 K and S_A from 5 to 70 g kg^{-1} as a function of temperature and salinity ($\sigma=0.0063 \text{ kg m}^{-3}$).

$$B = b_0 + b_1(T/K - 273.15) + b_2(T/K - 273.15)^2 \quad (5b)$$

$$C = c_0 \quad (5c)$$

The parameters needed to fit the seawater measurements ($N=242$) from 273.15 to 313.15 K and S_A from 5 to 50 (g kg^{-1}) are tabulated in Table 2 along with the standard error of the fit ($\sigma=0.0037 \text{ kg m}^{-3}$). This standard error of the 273.15 to 313.15 K fit is similar (Fig. 2) to the differences between our measurements and those calculated from the equation of state of seawater (Millero and Poisson, 1981). The parameters needed to fit the seawater measurements ($N=280$) from 298.15 to 363.15 K are also tabulated in Table 2 along with the standard error of the fit ($\sigma=0.0063 \text{ kg m}^{-3}$). All of the measurements from 273.15 to 363.15 K ($N=522$) have also been fitted to Eq. (5). The parameters for the fits are given in Table 2 along with the standard error of the fit ($\sigma=0.0063 \text{ kg m}^{-3}$). The differences between the measured and calculated densities from these fits are shown in Fig. 3. Most of the differences are within 2σ , where σ is the standard error of the fit. The errors appear to be larger at high temperatures, apparently due to difficulties in removing air from the samples. These measurements extend the equation of state to seawater as a function of the absolute salinity $S_A \text{ g kg}^{-1}$ over a wide range of temperature and salinity.

The measurements made in this study from 273.15 to 315.15 K and 273.15 to 363.15 K have been fitted to Eq. (5)

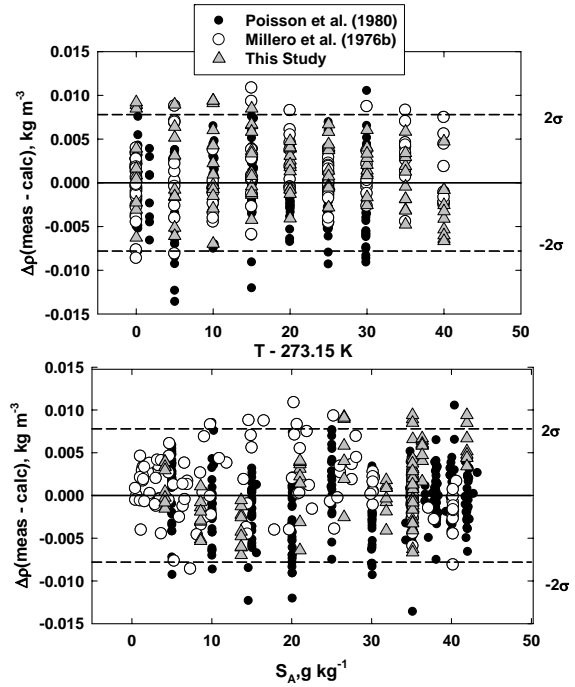


Fig. 4. The deviations between the measured ($N=713$) and calculated values from 273.15 to 313.15 K and S_A from 0 to 40 g kg^{-1} of Poisson et al. (1980), Millero et al. (1976b), and this study as a function of temperature and salinity ($\sigma=0.0037 \text{ kg m}^{-3}$).

with all of the measurements used to determine the International Equation of state of seawater (Millero et al., 1976b; Poisson et al., 1980). The results of these fits ($N=713$ from 273.15 to 313.15 K and $N=962$ from 273.15 to 363.15 K) are tabulated in Table 3 along with the standard errors, respectively $\sigma=0.0036 \text{ kg m}^{-3}$ and $\sigma=0.0063 \text{ kg m}^{-3}$. The differences between the measured and calculated densities from 273.15 to 313.15 K and 273.15 to 363.15 K are shown respectively, in Figs. 4 and 5. As with our other fits, most of the differences are within 2σ .

It should be pointed out that the earlier measurements (Millero et al., 1976b; Poisson et al., 1980) made on the 1968 temperature scale were converted to the 1990 temperature scale (Preston-Thomas, 1990). Changes in the temperature scale do not significantly affect the values of $(\rho-\rho^0)$ which do not vary much with temperature. The results of this study can be used to determine the properties of seawater and most estuarine waters over a wide range of Absolute Salinity and temperature. These results will also be useful in extending the ionic interaction model for seawater (Pierrot and Millero, 2000) to 363.15 K. Future work on the density of seawater above 373.15 K at applied pressure are needed to extend the temperature range to the levels available for the thermochemical properties of seawater (Millero and Pierrot, 2005; Feistel, 2008).

Table 2. The coefficients for the densities measured in this study fitted to Eq. (2).

| | 273.15 to 313.15 K | 298.15 to 363.15 K | 273.15 to 363.15 K |
|---------------------------|---------------------------|---------------------------|---------------------------|
| S_A | 8.246111E-01 | 8.055888E-01 | 8.174451E-01 |
| $S_A(T/K-273.15)$ | -3.956103E-03 | -2.588520E-03 | -3.638577E-03 |
| $S_A(T/K-273.15)^2$ | 7.274549E-05 | 2.449074E-05 | 6.480811E-05 |
| $S_A(T/K-273.15)^3$ | -8.239634E-07 | 3.908917E-08 | -7.312404E-07 |
| $S_A(T/K-273.15)^4$ | 5.332909E-09 | -1.795219E-09 | 5.330431E-09 |
| $S_A(T/K-273.15)^5$ | | 8.617570E-12 | -1.657628E-11 |
| $S_A^{1.5}$ | -6.006733E-03 | -4.893389E-03 | -5.481436E-03 |
| $S_A^{1.5}(T/K-273.15)$ | 7.970908E-05 | 2.132621E-05 | 3.486075E-05 |
| $S_A^{1.5}(T/K-273.15)^2$ | -1.018797E-06 | -1.907666E-07 | -3.049727E-07 |
| S_A^2 | 5.281399E-04 | 5.165275E-04 | 5.346196E-04 |
| Number | 242 | 280 | 522 |
| Std.Err.Fit | 0.0037 kg m ⁻³ | 0.0063 kg m ⁻³ | 0.0063 kg m ⁻³ |

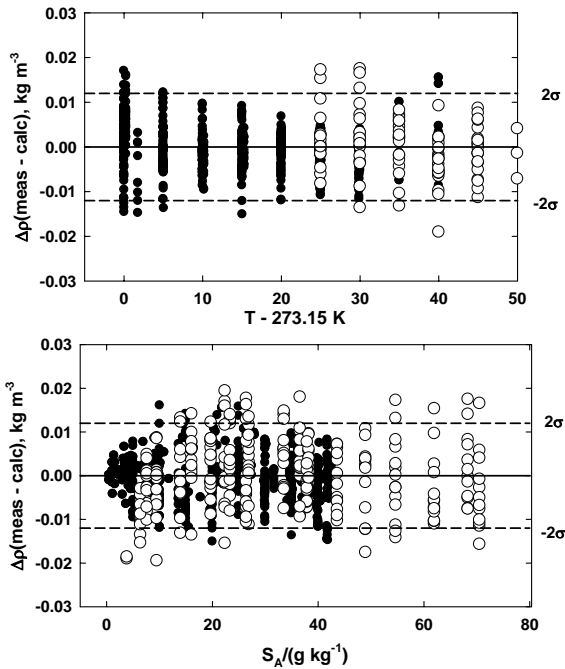


Fig. 5. The deviations between the measured ($N=962$) and calculated values from 273.15 to 363.15 K and S_A from 0 to 70 g kg⁻¹ as a function of temperature and salinity ($\sigma=0.0062$ kg m⁻³). The closed circles are from 273.15 to 313.15 K (Poisson et al., 1980; Millero et al., 1976b) and the open circles from this study are from 298.15 to 363.15 K.

Table 3. The coefficients for the densities measured in this study and literature data (Millero et al., 1976b; Poisson et al., 1980) fitted to Eq. (2).

| | 273.15 to 313.15 K | 273.15 to 363.15 K |
|---------------------------|---------------------------|---------------------------|
| S_A | 8.207423E-01 | 8.197247E-01 |
| $S_A(T/K-273.15)$ | -4.090059E-03 | -3.779454E-03 |
| $S_A(T/K-273.15)^2$ | 7.695554E-05 | 6.821795E-05 |
| $S_A(T/K-273.15)^3$ | -8.284116E-07 | -8.009571E-07 |
| $S_A(T/K-273.15)^4$ | 5.490137E-09 | 6.158885E-09 |
| $S_A(T/K-273.15)^5$ | | -2.001919E-11 |
| $S_A^{1.5}$ | -5.738085E-03 | -5.808305E-03 |
| $S_A^{1.5}(T/K-273.15)$ | 1.044735E-04 | 5.354872E-05 |
| $S_A^{1.5}(T/K-273.15)^2$ | -1.758636E-06 | -4.714602E-07 |
| S_A^2 | 4.840416E-04 | 5.249266E-04 |
| Number | 713 | 962 |
| Std.Err.Fit | 0.0036 kg m ⁻³ | 0.0063 kg m ⁻³ |

Table A1. The densities (kg m^{-3}) of seawater measured between 0 and 40°C.

| t | S_A | Meas | t | S_A | Meas | t | S_A | Meas |
|--------|---------------------|--------------------|--------|---------------------|--------------------|--------|---------------------|--------------------|
| °C | g kg^{-1} | kg m^{-3} | °C | g kg^{-1} | kg m^{-3} | °C | g kg^{-1} | kg m^{-3} |
| -0.002 | 31.837 | 25.587 | 10.004 | 35.157 ^a | 27.243 | 24.997 | 9.792 | 7.322 |
| 0.000 | 8.607 | 6.952 | 15.000 | 8.607 | 6.583 | 24.997 | 36.753 | 27.491 |
| 0.000 | 13.678 | 11.024 | 15.000 | 15.741 | 12.015 | 24.998 | 36.171 | 27.055 |
| 0.000 | 35.142 | 28.246 | 15.000 | 26.221 | 20.018 | 24.999 | 26.559 | 19.842 |
| 0.000 | 35.142 | 28.246 | 15.001 | 13.678 | 10.445 | 24.999 | 31.914 | 23.854 |
| 0.000 | 35.157 ^a | 28.251 | 15.001 | 21.037 | 16.064 | 24.999 | 35.168 | 26.298 |
| 0.000 | 35.157 ^a | 28.251 | 15.001 | 35.168 | 26.880 | 24.999 | 35.168 | 26.299 |
| 0.000 | 36.343 | 29.212 | 15.001 | 35.168 | 26.873 | 24.999 | 35.168 | 26.298 |
| 0.000 | 41.941 | 33.718 | 15.001 | 35.168 | 26.873 | 24.999 | 35.168 | 26.299 |
| 0.001 | 4.147 | 3.364 | 15.001 | 35.169 | 26.873 | 24.999 | 35.169 | 26.298 |
| 0.001 | 21.037 | 16.930 | 15.001 | 41.941 | 32.082 | 24.999 | 35.182 | 26.310 |
| 1.000 | 15.741 | 12.619 | 15.002 | 4.147 | 3.184 | 25.000 | 5.365 | 4.019 |
| 1.000 | 22.930 | 18.366 | 15.002 | 31.837 | 24.320 | 25.000 | 5.365 | 4.017 |
| 1.003 | 35.157 ^a | 28.134 | 15.002 | 35.157 ^a | 26.863 | 25.000 | 10.943 | 8.179 |
| 1.005 | 35.157 ^a | 28.140 | 15.002 | 36.343 | 27.781 | 25.000 | 15.741 | 11.756 |
| 4.999 | 41.941 | 33.064 | 15.003 | 35.132 | 26.854 | 25.000 | 17.706 | 13.219 |
| 5.000 | 10.943 | 8.651 | 15.003 | 35.142 | 26.854 | 25.000 | 17.706 | 13.226 |
| 5.000 | 15.741 | 12.420 | 15.003 | 35.142 | 26.854 | 25.000 | 22.930 | 17.124 |
| 5.000 | 31.837 | 25.083 | 15.004 | 35.157 ^a | 26.860 | 25.000 | 26.221 | 19.584 |
| 5.001 | 8.607 | 6.802 | 19.998 | 35.157 ^a | 26.550 | 25.000 | 26.221 | 19.589 |
| 5.001 | 13.678 | 10.790 | 19.998 | 35.157 ^a | 26.550 | 25.000 | 27.632 | 20.643 |
| 5.001 | 35.142 | 27.689 | 20.000 | 8.607 | 6.501 | 25.000 | 35.157 ^a | 26.290 |
| 5.001 | 35.142 | 27.689 | 20.000 | 10.943 | 8.263 | 25.000 | 35.157 ^a | 26.290 |
| 5.002 | 4.147 | 3.289 | 20.000 | 15.741 | 11.873 | 25.000 | 36.171 | 27.055 |
| 5.002 | 21.037 | 16.584 | 20.000 | 17.706 | 13.357 | 25.000 | 36.579 | 27.362 |
| 5.004 | 35.157 ^a | 27.711 | 20.000 | 22.930 | 17.291 | 25.001 | 4.147 | 3.111 |
| 5.005 | 35.157 ^a | 27.706 | 20.001 | 21.037 | 15.870 | 25.001 | 31.837 | 23.794 |
| 10.000 | 15.741 | 12.198 | 20.001 | 31.837 | 24.034 | 25.002 | 6.435 | 4.813 |
| 10.000 | 22.930 | 17.763 | 20.001 | 35.132 | 26.534 | 25.002 | 7.344 | 5.497 |
| 10.001 | 4.147 | 3.230 | 20.001 | 35.142 | 26.535 | 25.002 | 7.344 | 5.496 |
| 10.001 | 13.678 | 10.599 | 20.001 | 35.142 | 26.535 | 25.002 | 7.678 | 5.738 |
| 10.001 | 21.037 | 16.298 | 20.001 | 35.168 | 26.562 | 25.002 | 9.547 | 7.139 |
| 10.001 | 26.559 | 20.580 | 20.001 | 35.168 | 26.561 | 25.002 | 12.752 | 9.526 |
| 10.001 | 31.837 | 24.666 | 20.001 | 35.168 | 26.562 | 25.002 | 13.678 | 10.214 |
| 10.001 | 35.142 | 27.235 | 20.001 | 35.168 | 26.561 | 25.002 | 14.060 | 10.504 |
| 10.001 | 35.157 ^a | 27.240 | 20.001 | 35.169 | 26.561 | 25.002 | 19.183 | 14.325 |
| 10.001 | 35.168 | 27.257 | 20.002 | 4.147 | 3.144 | 25.002 | 19.183 | 14.325 |
| 10.001 | 35.168 | 27.252 | 20.002 | 13.678 | 10.319 | 25.002 | 21.037 | 15.710 |
| 10.001 | 35.168 | 27.257 | 20.002 | 36.343 | 27.455 | 25.002 | 22.843 | 17.059 |
| 10.001 | 35.168 | 27.252 | 20.002 | 41.941 | 31.710 | 25.002 | 23.478 | 17.529 |
| 10.001 | 35.169 | 27.252 | 20.003 | 35.157 ^a | 26.546 | 25.002 | 27.032 | 20.193 |
| 10.002 | 8.607 | 6.682 | 20.006 | 35.157 ^a | 26.550 | 25.002 | 31.832 | 23.791 |
| 10.002 | 41.941 | 32.530 | 24.995 | 22.487 | 16.791 | 25.002 | 35.132 | 26.274 |
| 10.003 | 35.157 ^a | 27.244 | 24.996 | 12.752 | 9.526 | 25.002 | 35.142 | 26.275 |
| 25.002 | 35.157 ^a | 26.296 | 30.005 | 68.654 | 51.393 | 40.000 | 35.157 ^a | 25.746 |
| 25.002 | 35.157 ^a | 26.286 | 30.006 | 9.547 | 7.078 | 40.000 | 35.157 ^a | 25.746 |
| 25.002 | 35.157 ^a | 26.296 | 30.006 | 70.871 | 53.089 | 40.001 | 21.037 | 15.378 |
| 25.002 | 35.157 ^a | 26.286 | 30.007 | 7.678 | 5.692 | 40.001 | 26.559 | 19.426 |
| 25.002 | 36.343 | 27.188 | 30.030 | 35.157 ^a | 26.069 | 40.001 | 36.343 | 26.625 |
| 25.002 | 41.941 | 31.401 | 30.030 | 35.157 ^a | 26.065 | 40.002 | 4.147 | 3.044 |

Table A1. Continued.

| t | S_A | Meas | t | S_A | Meas | t | S_A | Meas |
|--------|---------------------|--------------------|--------|---------------------|--------------------|--------|---------------------|--------------------|
| °C | g kg ⁻¹ | kg m ⁻³ | °C | g kg ⁻¹ | kg m ⁻³ | °C | g kg ⁻¹ | kg m ⁻³ |
| 25.003 | 19.821 | 14.800 | 34.997 | 35.157 ^a | 25.894 | 40.002 | 8.607 | 6.299 |
| 25.003 | 43.831 | 32.837 | 34.998 | 26.551 | 19.525 | 40.002 | 31.837 | 23.300 |
| 25.003 | 62.268 | 46.882 | 34.998 | 35.157 | 25.897 | 40.002 | 35.132 | 25.725 |
| 25.004 | 9.792 | 7.320 | 34.998 | 38.425 | 28.324 | 40.002 | 35.142 | 25.729 |
| 25.004 | 16.165 | 12.075 | 34.999 | 35.157 ^a | 25.892 | 40.002 | 35.142 | 25.729 |
| 25.004 | 22.843 | 17.060 | 34.999 | 35.157 ^a | 25.892 | 40.003 | 33.716 | 24.684 |
| 25.004 | 49.210 | 36.917 | 34.999 | 35.182 | 25.918 | 40.004 | 49.210 | 36.177 |
| 25.004 | 54.936 | 41.279 | 35.000 | 26.559 | 19.538 | 40.004 | 62.268 | 45.945 |
| 25.004 | 68.654 | 51.797 | 35.000 | 27.032 | 19.889 | 40.005 | 7.678 | 5.617 |
| 25.004 | 70.871 | 53.507 | 35.001 | 8.607 | 6.335 | 40.005 | 16.165 | 11.815 |
| 25.005 | 33.716 | 25.209 | 35.001 | 13.678 | 10.055 | 40.005 | 23.478 | 17.166 |
| 25.006 | 38.108 | 28.513 | 35.001 | 31.837 | 23.433 | 40.005 | 27.032 | 19.772 |
| 25.007 | 26.551 | 19.832 | 35.002 | 4.147 | 3.063 | 40.005 | 38.108 | 27.922 |
| 29.998 | 38.425 | 28.517 | 35.002 | 21.037 | 15.465 | 44.995 | 35.157 ^a | 25.637 |
| 29.999 | 35.182 | 26.094 | 35.002 | 35.132 | 25.875 | 44.995 | 35.157 ^a | 25.639 |
| 29.999 | 35.182 | 26.089 | 35.002 | 35.142 | 25.878 | 49.998 | 35.157 ^a | 25.564 |
| 30.001 | 8.607 | 6.381 | 35.002 | 35.142 | 25.878 | | | |
| 30.001 | 13.678 | 10.126 | 35.002 | 36.343 | 26.777 | | | |
| 30.001 | 21.037 | 15.576 | 35.002 | 36.753 | 27.082 | | | |
| 30.001 | 22.487 | 16.653 | 35.002 | 41.941 | 30.927 | | | |
| 30.001 | 26.559 | 19.675 | 35.003 | 22.487 | 16.536 | | | |
| 30.001 | 27.032 | 20.027 | 35.004 | 7.678 | 5.648 | | | |
| 30.001 | 35.157 ^a | 26.074 | 35.004 | 23.478 | 17.262 | | | |
| 30.001 | 35.157 ^a | 26.074 | 35.004 | 43.831 | 32.354 | | | |
| 30.001 | 36.343 | 26.963 | 35.005 | 9.547 | 7.027 | | | |
| 30.002 | 14.060 | 10.414 | 35.005 | 16.165 | 11.888 | | | |
| 30.002 | 31.837 | 23.598 | 35.005 | 19.821 | 14.569 | | | |
| 30.002 | 35.132 | 26.056 | 35.005 | 33.716 | 24.833 | | | |
| 30.002 | 35.142 | 26.059 | 35.005 | 38.108 | 28.084 | | | |
| 30.002 | 35.142 | 26.059 | 35.005 | 54.936 | 40.673 | | | |
| 30.003 | 4.147 | 3.084 | 35.005 | 62.268 | 46.202 | | | |
| 30.003 | 26.551 | 19.663 | 35.005 | 68.654 | 51.054 | | | |
| 30.003 | 43.831 | 32.573 | 35.005 | 70.871 | 52.739 | | | |
| 30.004 | 16.165 | 11.970 | 39.995 | 35.157 ^a | 25.747 | | | |
| 30.004 | 19.821 | 14.667 | 39.996 | 35.157 ^a | 25.748 | | | |
| 30.004 | 23.478 | 17.384 | 39.996 | 36.753 | 26.929 | | | |
| 30.005 | 33.716 | 25.005 | 39.998 | 38.425 | 28.161 | | | |
| 30.005 | 36.753 | 27.269 | 39.999 | 43.831 | 32.162 | | | |

^a Measurements made on Standard Seawater ($S_A=35.157$ g kg⁻¹).

Table B1. The densities (kg m^{-3}) of seawater measured between 25 and 90°C.

| t | S_A | Meas | t | S_A | Meas | t | S_A | Meas |
|--------|--------------------|--------------------|--------|--------------------|--------------------|--------|--------------------|--------------------|
| °C | g kg^{-1} | kg m^{-3} | °C | g kg^{-1} | kg m^{-3} | °C | g kg^{-1} | kg m^{-3} |
| 24.995 | 22.487 | 16.791 | 35.003 | 22.487 | 16.536 | 45.005 | 6.435 | 4.680 |
| 24.996 | 38.425 | 28.753 | 35.004 | 6.435 | 4.731 | 45.005 | 7.678 | 5.592 |
| 24.997 | 36.753 | 27.491 | 35.004 | 7.678 | 5.648 | 45.005 | 16.165 | 11.765 |
| 25.002 | 6.435 | 4.813 | 35.004 | 23.478 | 17.262 | 45.005 | 23.478 | 17.084 |
| 25.002 | 7.678 | 5.738 | 35.004 | 43.831 | 32.354 | 45.005 | 27.032 | 19.683 |
| 25.002 | 9.547 | 7.139 | 35.005 | 9.547 | 7.027 | 45.005 | 33.716 | 24.578 |
| 25.002 | 14.060 | 10.504 | 35.005 | 16.165 | 11.888 | 45.005 | 68.654 | 50.547 |
| 25.002 | 23.478 | 17.529 | 35.005 | 19.821 | 14.569 | 45.005 | 70.871 | 52.218 |
| 25.002 | 27.032 | 20.193 | 35.005 | 33.716 | 24.833 | 45.006 | 22.487 | 16.358 |
| 25.003 | 19.821 | 14.800 | 35.005 | 38.108 | 28.084 | 45.006 | 38.108 | 27.796 |
| 25.003 | 43.831 | 32.837 | 35.005 | 54.936 | 40.673 | 49.995 | 22.487 | 16.302 |
| 25.003 | 62.268 | 46.882 | 35.005 | 62.268 | 46.202 | 49.995 | 26.551 | 19.246 |
| 25.004 | 16.165 | 12.075 | 35.005 | 68.654 | 51.054 | 49.997 | 14.060 | 10.187 |
| 25.004 | 49.210 | 36.917 | 35.005 | 70.871 | 52.739 | 50.001 | 36.753 | 26.710 |
| 25.004 | 54.936 | 41.279 | 39.992 | 26.551 | 19.413 | 50.001 | 54.936 | 40.106 |
| 25.004 | 68.654 | 51.797 | 39.996 | 36.753 | 26.929 | 50.002 | 9.547 | 6.931 |
| 25.004 | 70.871 | 53.507 | 39.997 | 14.060 | 10.268 | 50.002 | 43.831 | 31.902 |
| 25.005 | 33.716 | 25.209 | 39.998 | 9.547 | 6.977 | 50.003 | 16.165 | 11.712 |
| 25.006 | 38.108 | 28.513 | 39.998 | 38.425 | 28.161 | 50.004 | 19.821 | 14.361 |
| 25.007 | 26.551 | 19.832 | 39.999 | 43.831 | 32.162 | 50.004 | 38.425 | 27.933 |
| 29.998 | 38.425 | 28.517 | 40.000 | 22.487 | 16.437 | 50.004 | 68.654 | 50.367 |
| 30.001 | 22.487 | 16.653 | 40.002 | 6.435 | 4.702 | 50.005 | 6.435 | 4.664 |
| 30.001 | 27.032 | 20.027 | 40.003 | 33.716 | 24.684 | 50.005 | 7.678 | 5.564 |
| 30.002 | 14.060 | 10.414 | 40.004 | 19.821 | 14.481 | 50.005 | 23.478 | 17.024 |
| 30.003 | 26.551 | 19.663 | 40.004 | 49.210 | 36.177 | 50.005 | 27.032 | 19.611 |
| 30.003 | 43.831 | 32.573 | 40.004 | 62.268 | 45.945 | 50.006 | 33.716 | 24.486 |
| 30.004 | 6.435 | 4.763 | 40.005 | 7.678 | 5.617 | 50.006 | 38.108 | 27.690 |
| 30.004 | 16.165 | 11.970 | 40.005 | 16.165 | 11.815 | 50.006 | 49.210 | 35.877 |
| 30.004 | 19.821 | 14.667 | 40.005 | 23.478 | 17.166 | 50.006 | 62.268 | 45.575 |
| 30.004 | 23.478 | 17.384 | 40.005 | 27.032 | 19.772 | 50.006 | 70.871 | 52.027 |
| 30.004 | 54.936 | 40.949 | 40.005 | 38.108 | 27.922 | 54.996 | 26.551 | 19.206 |
| 30.004 | 62.268 | 46.511 | 40.005 | 54.936 | 40.440 | 55.001 | 14.060 | 10.163 |
| 30.005 | 33.716 | 25.005 | 40.005 | 68.654 | 50.774 | 55.001 | 22.487 | 16.268 |
| 30.005 | 36.753 | 27.269 | 40.005 | 70.871 | 52.451 | 55.001 | 43.831 | 31.818 |
| 30.005 | 38.108 | 28.280 | 44.994 | 36.753 | 26.805 | 55.003 | 36.753 | 26.639 |
| 30.005 | 68.654 | 51.393 | 44.998 | 14.060 | 10.224 | 55.004 | 9.547 | 6.903 |
| 30.006 | 9.547 | 7.078 | 45.001 | 38.425 | 28.034 | 55.004 | 38.425 | 27.857 |
| 30.006 | 70.871 | 53.089 | 45.002 | 26.551 | 19.324 | 55.004 | 68.654 | 50.229 |
| 30.007 | 7.678 | 5.692 | 45.002 | 62.268 | 45.741 | 55.005 | 7.678 | 5.559 |
| 34.998 | 14.060 | 10.326 | 45.003 | 43.831 | 32.021 | 55.005 | 19.821 | 14.325 |
| 34.998 | 26.551 | 19.525 | 45.004 | 9.547 | 6.958 | 55.005 | 23.478 | 16.972 |
| 34.998 | 38.425 | 28.324 | 45.004 | 19.821 | 14.416 | 55.005 | 27.032 | 19.559 |
| 35.000 | 27.032 | 19.889 | 45.004 | 49.210 | 36.009 | 55.005 | 70.871 | 51.889 |
| 35.002 | 36.753 | 27.082 | 45.004 | 54.936 | 40.253 | 55.006 | 6.435 | 4.653 |
| 55.006 | 16.165 | 11.681 | 65.005 | 49.210 | 35.654 | 80.001 | 38.425 | 27.764 |
| 55.006 | 33.716 | 24.416 | 65.005 | 68.654 | 50.067 | 80.001 | 43.831 | 31.703 |
| 55.006 | 38.108 | 27.618 | 69.999 | 26.551 | 19.142 | 80.002 | 6.435 | 4.640 |
| 55.006 | 49.210 | 35.778 | 70.000 | 22.487 | 16.210 | 80.002 | 7.678 | 5.540 |
| 55.006 | 54.936 | 40.006 | 70.000 | 38.425 | 27.753 | 80.002 | 9.547 | 6.885 |
| 55.006 | 62.268 | 45.450 | 70.001 | 33.716 | 24.326 | 80.002 | 19.821 | 14.294 |
| 59.998 | 26.551 | 19.172 | 70.001 | 54.936 | 39.852 | 80.002 | 22.487 | 16.202 |
| 59.999 | 14.060 | 10.152 | 70.002 | 9.547 | 6.878 | 80.002 | 27.032 | 19.482 |

Table B1. Continued .

| <i>t</i> | <i>S_A</i> | Meas | <i>t</i> | <i>S_A</i> | Meas | <i>t</i> | <i>S_A</i> | Meas |
|----------|----------------------|--------------------|----------|----------------------|--------------------|----------|----------------------|--------------------|
| °C | g kg ⁻¹ | kg m ⁻³ | °C | g kg ⁻¹ | kg m ⁻³ | °C | g kg ⁻¹ | kg m ⁻³ |
| 60.001 | 7.678 | 5.544 | 70.002 | 23.478 | 16.919 | 80.002 | 33.716 | 24.336 |
| 60.001 | 33.716 | 24.376 | 70.002 | 27.032 | 19.475 | 80.003 | 54.936 | 39.868 |
| 60.001 | 68.654 | 50.130 | 70.002 | 36.753 | 26.537 | 80.004 | 23.478 | 16.928 |
| 60.002 | 9.547 | 6.889 | 70.002 | 38.108 | 27.520 | 80.004 | 38.108 | 27.536 |
| 60.002 | 36.753 | 26.583 | 70.002 | 43.831 | 31.695 | 80.004 | 49.210 | 35.641 |
| 60.003 | 19.821 | 14.299 | 70.002 | 49.210 | 35.635 | 80.004 | 70.871 | 51.700 |
| 60.003 | 22.487 | 16.234 | 70.002 | 62.268 | 45.278 | 80.006 | 62.268 | 45.285 |
| 60.003 | 38.425 | 27.801 | 70.002 | 70.871 | 51.684 | 80.006 | 68.654 | 50.052 |
| 60.004 | 49.210 | 35.706 | 70.003 | 6.435 | 4.630 | 85.000 | 22.487 | 16.224 |
| 60.005 | 23.478 | 16.947 | 70.003 | 19.821 | 14.281 | 85.000 | 36.753 | 26.569 |
| 60.005 | 43.831 | 31.744 | 70.004 | 7.678 | 5.532 | 85.001 | 19.821 | 14.311 |
| 60.005 | 62.268 | 45.363 | 70.004 | 16.165 | 11.644 | 85.001 | 26.551 | 19.160 |
| 60.005 | 70.871 | 51.785 | 70.004 | 68.654 | 50.036 | 85.002 | 23.478 | 16.947 |
| 60.006 | 6.435 | 4.645 | 74.994 | 14.060 | 10.132 | 85.002 | 33.716 | 24.361 |
| 60.006 | 16.165 | 11.661 | 75.000 | 22.487 | 16.206 | 85.002 | 38.108 | 27.563 |
| 60.006 | 27.032 | 19.517 | 75.000 | 36.753 | 26.531 | 85.002 | 38.425 | 27.796 |
| 60.006 | 38.108 | 27.557 | 75.002 | 9.547 | 6.874 | 85.002 | 43.831 | 31.736 |
| 60.006 | 54.936 | 39.915 | 75.002 | 26.551 | 19.126 | 85.002 | 68.654 | 50.100 |
| 64.999 | 9.547 | 6.875 | 75.003 | 68.654 | 50.028 | 85.002 | 70.871 | 51.745 |
| 64.999 | 14.060 | 10.139 | 75.004 | 19.821 | 14.281 | 85.003 | 7.678 | 5.557 |
| 64.999 | 26.551 | 19.153 | 75.004 | 38.425 | 27.750 | 85.003 | 9.547 | 6.890 |
| 65.001 | 36.753 | 26.559 | 75.005 | 16.165 | 11.654 | 85.003 | 16.165 | 11.675 |
| 65.002 | 22.487 | 16.218 | 75.005 | 49.210 | 35.626 | 85.003 | 27.032 | 19.512 |
| 65.003 | 19.821 | 14.283 | 75.005 | 54.936 | 39.845 | 85.003 | 49.210 | 35.672 |
| 65.003 | 38.425 | 27.769 | 75.005 | 62.268 | 45.263 | 85.003 | 62.268 | 45.325 |
| 65.004 | 6.435 | 4.636 | 75.006 | 6.435 | 4.628 | 85.004 | 14.060 | 10.148 |
| 65.004 | 16.165 | 11.651 | 75.006 | 7.678 | 5.527 | 85.004 | 54.936 | 39.899 |
| 65.004 | 27.032 | 19.497 | 75.006 | 23.478 | 16.924 | 89.996 | 9.547 | 6.895 |
| 65.004 | 33.716 | 24.346 | 75.006 | 27.032 | 19.478 | 89.998 | 14.060 | 10.168 |
| 65.004 | 43.831 | 31.703 | 75.006 | 33.716 | 24.334 | 89.998 | 62.268 | 45.412 |
| 65.004 | 54.936 | 39.877 | 75.006 | 38.108 | 27.516 | 89.999 | 7.678 | 5.558 |
| 65.004 | 62.268 | 45.304 | 75.006 | 43.831 | 31.681 | 89.999 | 16.165 | 11.678 |
| 65.004 | 70.871 | 51.716 | 75.006 | 70.871 | 51.675 | 89.999 | 33.716 | 24.404 |
| 65.005 | 7.678 | 5.537 | 79.993 | 14.060 | 10.132 | 89.999 | 38.108 | 27.604 |
| 65.005 | 23.478 | 16.927 | 79.998 | 26.551 | 19.139 | 89.999 | 49.210 | 35.725 |
| 65.005 | 38.108 | 27.522 | 80.000 | 36.753 | 26.538 | 89.999 | 54.936 | 39.964 |
| 89.999 | 70.871 | 51.824 | | | | | | |
| 90.000 | 23.478 | 16.970 | | | | | | |
| 90.001 | 26.551 | 19.194 | | | | | | |
| 90.001 | 36.753 | 26.612 | | | | | | |
| 90.002 | 38.425 | 27.838 | | | | | | |
| 90.003 | 19.821 | 14.332 | | | | | | |
| 90.003 | 22.487 | 16.245 | | | | | | |
| 89.999 | 49.210 | 35.725 | | | | | | |
| 89.999 | 54.936 | 39.964 | | | | | | |
| 89.999 | 70.871 | 51.824 | | | | | | |
| 90.000 | 23.478 | 16.970 | | | | | | |
| 90.001 | 26.551 | 19.194 | | | | | | |
| 90.001 | 36.753 | 26.612 | | | | | | |
| 90.002 | 38.425 | 27.838 | | | | | | |
| 90.003 | 19.821 | 14.332 | | | | | | |
| 90.003 | 22.487 | 16.245 | | | | | | |

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References

- Bigg, P. H.: Density of water in SI units over the range 0–40°C, *Brit. J. Appl. Phys.*, 18, 521–524, 1967.
- Brewer, P. G. and Bradshaw, A.: The effect of non-ideal composition of seawater on salinity and density, *J. Mar. Res.*, 33, 157–175, 1975.
- Feistel, R.: A Gibbs function for seawater thermodynamics from –6 to 80°C and salinity up to 120 g kg⁻¹, *Deep-Sea Part I*, 55(12), 1639–1671, doi:10.1016/j.dsr.2008.07.004, 2008.
- Kell, G. S.: The density, thermal expansivity and compressibility of liquid water from 0 to 150°C: correlations and tables for atmospheric pressure and saturation reviewed and expressed on the 1968 temperature scale, *J. Chem. Eng. Data*, 20, 97–105, 1975.
- Millero, F. J.: Effect of changes in the composition of seawater on the density-salinity relationship, *Deep-Sea Res. Part I*, 47, 1583–1590, 2000.
- Millero, F. J. and Kremling, K.: The densities of Baltic Sea waters, *Deep-Sea Res.*, 23, 1129–1138, 1976.
- Millero, F. J. and Pierrot, D.: The thermochemical properties of seawater fit to the Pitzer equations, *Mar. Chem.*, 94, 81–99, 2005.
- Millero, F. J. and Poisson, A.: International one-atmosphere equation of state of seawater, *Deep-Sea Res.*, 28, 625–629, 1981.
- Millero, F. J., Chetirkin, P. V., and Culkin, F.: The relative conductivity and density of standard seawaters, *Deep-Sea Res.*, 24, 315–321, 1976a.
- Millero, F. J., Gonzalez, A., and Ward, G. K.: The density of seawater solutions at on atmosphere as a function of temperature and salinity, *J. Mar. Res.*, 34, 61–93, 1976b.
- Millero, F. J., Forsht, D., Means, D., Giekes, J., and Kenyon, K.: The density of North Pacific Ocean waters, *J. Geophys. Res.*, 83, 2359–2364, 1978.
- Millero, F. J., Waters, J., Woosley, R., Huang, F., and Chanson, M.: The effect of composition of the density of Indian Ocean waters, *Deep-Sea Res. Part I*, 55, 960–470, 2008a.
- Millero, F. J., Feistel, R., Wright, D. G., and McDougall, T. J.: The composition of Standard Seawater and the definition of the Reference-Composition Salinity Scale, *Deep-Sea Res. Part I*, 55, 50–72, 2008b.
- Millero, F. J., Huang, F., Williams, N., Waters, J., and Woosley, R.: The effect of composition on the density of South Pacific Ocean waters, *Mar. Chem.*, in press, 2009.
- Pierrot, D. and Millero, F. J.: The apparent molal volume and compressibility of seawater fit to the Pitzer equations, *J. Solution Chem.*, 29, 719–742, 2000.
- Poisson, A. and Gadhomi, M. H.: An extension of the Practical Salinity Scale 1987 and the Equation of State 1980 to high salinities, *Deep-Sea Res.*, 40, 1689–1698, 1993.
- Poisson, A., Brunet, C., and Brun-Cottan, J. C.: Density of standard seawater solutions at atmospheric pressure, *Deep-Sea Res.*, 27(12A), 1013–1028, 1980.
- Poisson, A., Lebel, J., and Brunet, C.: The densities of western Indian Ocean, Red Sea and eastern Mediterranean surface waters, *Deep-Sea Res.*, 28, 1161–1172, 1981.
- Preston-Thomas, H.: The international Temperature Scale of 1990 (ITS-90), *Metrologia*, 27, 3–10, 1990.
- Spieweck, F. and Bettin, H.: Review: Solid and liquid density determination. *Technisches Messen*, 59, 285–292, 1992.